

Subject card

Subject name and code	Elementary Functions, PG_00155432						
Field of study	Mathematics						
Date of commencement of studies	October 2025		Academic year of realisation of subject		2026/2027		
Education level	Master's studies		Subject group		Optional subject group Specialty subject group		
Mode of study	full-time studies		Mode of delivery		at the university		
Year of study	2		Language of instruction		Polish		
Semester of study	3		ECTS credits		6.0		
Learning profile	academic		Assessment form		exam		
Conducting unit	Institute of Mathematics -> Faculty of Mathematics, Physics and Informatics -> Rector						
Name and surname of lecturer (lecturers)	Subject supervisor		dr Agnieszka Demby				
	Teachers						
Lesson types	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	30.0	0.0	0.0	0.0	60
	E-learning hours included: 0.0						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan		Participation in consultation hours		Self-study	SUM
	Number of study hours	60		10.0		80.0	150
Subject objectives	Supplementing and deepening knowledge and skills from secondary school by: defining and introducing new types of elementary functions, studying functions using various methods, computer visualization of selected issues, solving more difficult or unusual tasks, linking with other areas of science or life.						
	Deepening the student's theoretical awareness of functions, i.e. e.g. the ability to link techniques for solving problems from high school with the properties of functions, proving skills.						

Learning outcomes	Course outcome	Subject outcome	Method of verification
	[MATMU2_W03] knows and understands in-depth a selected field of theoretical or applied mathematics and is able to understand the formulations of issues in this field that are still at the research stage and knows the connections of issues in this field with other areas of mathematics	Knows and understands in depth the classifications and properties of elementary functions and is able to understand the formulations of problems in this field that are still at the research stage, as well as knows the connections between problems in this field and other areas of mathematics, especially analysis and algebra.	[SW4] test/exam - oral or written [SW1] oral statement/ conversation/discussion
	[MATMU2_K02] is ready to precisely formulate questions to deepen his/her understanding of a given topic or find missing elements of reasoning	Is ready to formulate precise questions that serve to deepen one's understanding of a given topic or to find missing elements of reasoning regarding the objectives and content of the subject.	[SK8] observation of student's independent or team work
	[MATMU2_W01] knows and understands in-depth the theory of selected areas of mathematics	Knows and understands in an in-depth way the theory related to elementary functions and their various subtypes; knows examples of non-elementary functions, including selected theorems defining certain classes of non-elementary integrals; knows the applications of elementary functions outside mathematics and in real-life situations.	[SW4] test/exam - oral or written [SW2] presentation/project/paper/ report
	[MATMU2_K05] is ready to independently search for information in literature, also in foreign languages	Is ready to independently search for information in the literature, including in foreign languages, within the scope of the objectives and content of the subject.	[SK8] observation of student's independent or team work
	[MATMU2_K06] is ready to formulate opinions on basic mathematical issues	Is ready to formulate opinions on basic mathematical issues within the scope of the subject objectives and content.	[SK8] observation of student's independent or team work
	[MATMU2_W02] knows and understands well the role and importance of the construction of mathematical reasoning	Knows and understands well the role and importance of the construction of mathematical reasoning related to the properties of elementary functions.	[SW4] test/exam - oral or written [SW2] presentation/project/paper/ report
	[MATMU2_K04] is ready to understand and appreciate the importance of intellectual honesty in one's own and other people's actions; ethical conduct	Is ready to understand and appreciate the importance of intellectual honesty in one's own and others' actions; ethical conduct.	[SK8] observation of student's independent or team work
	[MATMU2_K01] is willing to acknowledge the limitations of his or her own knowledge and is willing to pursue further education	Is willing to acknowledge the limitations of his/her own knowledge and to engage in further education regarding the objectives and content of the subject.	[SK8] observation of student's independent or team work
	[MATMU2_U06] is able to apply methods and examples from a selected field of mathematics in related fields	Is able to investigate elementary functions using various methods, combining skills from mathematical analysis, algebra, and analytic geometry; is able to use computer visualization of various issues related to functions.	[SU1] oral statement/conversation/ discussion [SU2] presentation/project/paper/ report
	[MATMU2_U01] can construct mathematical reasoning: prove theorems and refute hypotheses through construction and selection of counterexamples	Is able to construct mathematical reasoning: prove the properties of functions using definitions and theorems from the lecture; is able to solve various types of tasks concerning elementary functions, including tasks from the canon of the extended secondary school leaving examination in mathematics.	[SU1] oral statement/conversation/ discussion [SU4] test/exam - oral or written
	[MATMU2_W06] knows and understands the principles of occupational health and safety sufficient to work independently as a mathematician	Knows and understands the principles of occupational health and safety to a degree sufficient to work independently as a mathematician.	[SW1] oral statement/ conversation/discussion

Subject contents	1. Recursive method of constructing a set of elementary functions (one real variable with real values). Proofs of elementary functions; examples of non-elementary functions. Algebraic and transcendental functions. 2. Review of algebraic functions - graphs, properties, applications outside mathematics. Selected theorems about polynomials, including solving polynomial equations by radicals. Solving rational and irrational equations and inequalities (referring to the properties of these functions). Parameter problems. 3. Power with a real exponent. Selected theorems about irrational numbers and powers. Power, exponential and logarithmic functions - graphs, properties, applications. 4. Trigonometric functions (including cotangent, secant and cosecant functions). Examples of approaches other than traditional ones, e.g. historical (segments related to the unit circle) or axiomatic. Graphs, properties, formulas, applications outside mathematics. Solving various types of trigonometric equations and inequalities. 5. Trigonometric functions - graphs, properties, formulas, applications. Examples of composition of trigonometric and trigonometric functions. 6. Elements of mathematical analysis: limit of elementary function, continuity (note about different definitions), derivative, differentiability, antiderivative (not necessarily elementary). Solving problems, including optimization and with a parameter. 7. Hyperbolic functions and area. Graphs, properties, formulas, applications outside mathematics. Analogies of formulas for trigonometric and hyperbolic functions, trigonometric functions and area, including formulas for derivatives. Formulas for calculating integrals containing the square root of x^2+1 or x^2-1. 8. Examples of elementary functions of a real variable with complex values. Theorems defining certain classes of elementary and non-elementary integrals. Visualization of the shape and position of a graph and various issues related to the study of elementary functions using computer programs, especially GeoGebra.																				
Prerequisites and co-requisites																					
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Example issues/ example questions/ tasks being completed	Give 5 examples of practical applications of elementary functions. (This refers to functional dependencies with a variable argument, and not, for example, calculating the square root of a specific number or the length of a certain segment using a trigonometric function in a specific geometric figure.)																				
Work placement	Not applicable																				

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